## An Introduction to Aldor and its Type System

Martin Dunstan

Numerical Algorithms Group (NAG Ltd)
and
Division of Computer Science
University of St. Andrews

#### Road Map

- What is Aldor?
- Introduction to syntax and basic concepts
- constants, variables and literals
- functions, iteration and generators
- categories and domains
- Inheritance of Categories and DomainsResolving overloading and extensions
- Conclusions

#### What is Aldor?

- Strongly-typed, imperative language with:
- two-level object model with inheritance (c.f. Haskell)
- overloading of symbol names
- types and functions are (constant) values
- generators, post facto extensions, literals etc.
- Foreign language interface:
- LISP (for AXIOM)
- C, C++, Fortran 77
- Automatic garbage collection (mark and sweep)
- Compiles to FOAM, LISP or C

# Constants, Variables and Literals

```
+++ PI: a well-known constant
PI == 3.1415926535_897932385;

ThisYear == 1999;
++ The current year
+++ Who am I?
MyName == "Martin Dunstan";

-- Variables are treated likewise
fortyTwo := 42;
```

### Simple Functions

```
fib == (n:Integer):Integer +-> {
    if (n < 2) then 1
    else fib(n - 1) + fib(n - 2);
}

-- More traditional definition
fib(n:Integer):Integer == {
    if (n < 2) then 1;
    else fib(n - 1) + fib(n - 2);
}

-- Bounded, polymorphic, curried function
Add(R:Ring)(a:R)(b:R):R == a + b;</pre>
```

## Looping and Iteration

```
-- Simple conditional loop
while (i < 10) repeat doSomething(i);
-- Bounded iteration
for i in 1..10 repeat doSomething(i);
-- Unbounded iteration
for i in 1.. repeat doSomething(i);
while (notDone) repeat
notDone := testIt(i);</pre>
```

## Generators (Coroutines)

```
primeStream == generate {
tenPrimes := [p for p in firstPrimes 10]
                                                                                                                                                                                                                          firstPrimes(n:Z):Generator(Z) == generate {
                                -- Construct a list of the first ten primes
                                                                                                                                                                                                                                                                                                                     for i in 1.. repeat
  if (prime? i) then yield i;
                                                                                                                                                          for prime in primeStream for total in 1..n repeat
                                                                                                                            yield prime;
```

#### Categories

- What are they?
- similar to Haskell type classes
- define the interface of domains
- values of type Category
- Particular features
- write categories first, then domains
- often parameterised: Aggregate(T:Type)
- -conditional: if (C has Order) then
- special symbol % for domain implemented

### A Simple Category

```
define Logic:Category == with {
                                                                   xor: . . .
BasicType;
                                                                 (%, %)-> %; ++ Logical 'meet', e.g. 'and'
(%, %)-> %; ++ Logical 'join', e.g. 'or'
(%, %)-> %; ++ `Exclusive or'
                                                                                                                  -> %; ++ Logical complement
```

## A More Complex Category

```
map :
apply :
                                           default {
                                                                                                   bracket:
            empty():% == [];
map(f:(S,S)->S, a:%, b:%):% ==
                                                                                                     Tuple S
[f(x,y) \text{ for } x \text{ in a for } y \text{ in b}];
                                                                                     ((S,S)->S, %, %) -> %;
                                                                      (%, SingleInteger)-> S;
```

## **Category Documentation**

```
++
                                                                                                                                                                                                                                                              ++
                                                                                                                                                                                                                                                                                               +
+
Rng():Category == Join(AbelianGroup, SemiGroup);
                                                              ++ Conditional attributes:
                                                                                                                                                                                                                                                                                                                                                          ++ Description:
                                                                                                                                                               Axioms:
                                spadnoZeroDivisors
                                                                                                                             x*(y+z) = x*y + x*z
                                                                                                                                                                                        group and a semigroup, with multiplication distributing over addition.
                                                                                                                                                                                                                                                            with a 1. This is a combination of an abelian
                                                                                                                                                                                                                                                                                       necessarily commutative, and not necessarily
                                                                                              (x+y)*z = x*z + y*z
                                                                                                                                                                                                                                                                                                                        The category of associative rings, not
                                   ab = 0 => a=0 \text{ or } b=0
```

#### **Domains**

- What are they?
- collections of exported constants
- abstract data types or packages
- public view (interface) defined by category
- Particular features
- often parameterised: Zmod(n:Integer)
- category often written with domain
- conditional definitions

### A Simple Domain

```
define ZmodCat(n:Integer):Category == Ring with {
  if (prime? n) then Field;
                                                                                                                                                                Zmod(n:Integer):ZmodCat(n) == add {
per mod((rep a) + (rep b), n);
if (prime? n) then {
  inv(x:%):% == ...
                                                                                                                                     Rep == Integer;
                                                                                (a:%) + (b:%):% ==
```

### **Complex Numbers**

```
== add {
                                                                                                                                       real :
                                          complex(r:R, i:R):% == per [r, i];
                                                                          import from Rep;
                                                                                          Rep == Record(real:R, imag:R);
               (r:R)*(c:%):% == complex(r*real c, r*imag c);
                                                                                                                         imag
-- (Other exports omitted ...)
                                                                                                                                         -> R;
                                                                                                                          -> 尺;
```

## Post facto Extensions

- What are they?
- a way of changing the behaviour of existing domains without modifying existing code
- Benefits
- prevent explosion of domains
- incremental library development
- allow for future development

### Inheritance in Aldor

- Categories
- multiple inheritance
- union of exports; disjunction of conditions
- Join $(C_1, C_2, ..., C_n) \equiv$ with  $\{C_1; C_2; ...; C_n\}$
- Domains
- single inheritance
- representations must be consistent
- ParentDom add ChildDom

# Binding: Resolving Overloading

- Searching for export op in domain dom:
- two passes, first pass ignoring all defaults
- first look for op in dom
- try parent of dom (skipping defaults)
- domain dom extended (skipping defaults)
- try the defaults of dom
- try the defaults of parent

try the defaults of domain extended

<sup>&</sup>lt;sup>†</sup>See the notes at end of the talk.

## Foreign Language Interface

```
import {
    getenv: String -> String;
    puts: String -> SingleInteger;
                                                                                                             export {
  fib: SingleInteger -> SingleInteger;
                     import {
   senddbl: (DoubleFloat -> DoubleFloat) -> ();
                                                                                        to Foreign C;
                                                                                                                                                                                from Foreign C;
from Foreign Fortran;
```

#### Conclusions

- Compiler
- generates efficient code (comparable to C)
- FOAM provides platform independance
- variety of platforms: UNIX, VMS, PC
- Language
- ideal for computer algebra implementations
- types and functions first class
- categories permit bounded polymorphism
- generators provide general iteration

- Things not mentioned:
- exceptions, case statements

default arguments for functions, records

- conversion of literals at runtime
- cross products, enumerations, records
- coerce, retract, restrict, qualify interactive use of compiler

#### **Some Comments**

After answering the questions that followed my talk two points sprang to mind that I would like to note:

- late binding would prevent the compiler performing important optimisations such as inlining so we don't do it. The compiler will bind references to identifiers as soon as possible. This can be delayed by using defaults in category definitions.
- the qualify "operator" (export\$Domain) can be used to pin down the domain that an export comes from. You still have to work out which export is actually invoked if your domain is the result of extending or inheriting from other domains. If your categories often use defaults then life is slightly harder.
- resolving binding of exports is tricky to explain in a single slide so I'll
  explain it more fully here. To look for the export op in the domain
  Dom we apply the following algorithm twice: the first time defaults are
  ignored, the second time they aren't:
- 1. see if op is in Dom
- 2. see if op is in the parent of Dom
- 3. see if op is in the domain that Dom extended

The important point is that this is recursive: to achieve step 2 we need to look in the parent of Dom (apply step 1), the parent of the parent of Dom (apply step 2) and so on before we can apply step 3. As soon as an export is found we stop.